

10. (10 pts) Suppose $V(t)$ is the value of a stock portfolio, where t is the time in years since January 1, 2000. Give a practical interpretation (using sentences about the portfolio), of the following numbers.

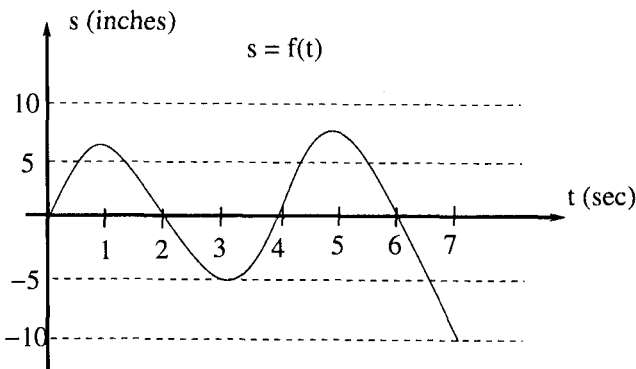
(a) $V(1.5) = 90,000$ at the end of June 2001, the value is \$90,000

(b) $V'(1) = 10,000$ at the end of 2000/beginning 2001, the value is increasing at a rate of \$10,000/year

(c) $V'(3)$ is positive and $V''(3)$ is negative
at the end of 2002/beginning of 2003, the value is increasing, but more slowly than it has been previously

(d) $V^{-1}(100,000) = 2$
at the end of 2001/beginning of 2002, the value is \$100,000

11. (10 pts) A marble is rolling back and forth along a rail. Let O denote a fixed point on the rail, and let $s = f(t)$ denote the marble's position (in inches) relative to O at time t (in seconds). s is positive to the right of the point O and negative to the left of O . The graph of the function $s = f(t)$ is given below.



(a) What is the average velocity of the marble over the first 7 seconds? avg. velocity = $\frac{-10-0}{7} = \frac{-10}{7}$

b) On which time intervals is the marble rolling to the right? the marble rolls to the right for $0 \leq t \leq 1$ and $3 \leq t \leq 5$. this is where f is increasing.

c) On which time intervals is the marble rolling to the left? rolls to the left for $1 \leq t \leq 2$ and $5 \leq t \leq 7$. this is where f is decreasing.

d) On which time intervals does the marble exhibit positive acceleration? negative?
pos. acceleration $\Leftrightarrow f'' > 0 \Leftrightarrow$ graph is concave up
 $\Leftrightarrow 2 \leq t \leq 4$

e) On which time intervals is the marble speeding up? slowing down?
speeding up \Leftrightarrow speed is increasing $\Leftrightarrow f'' > 0 \Leftrightarrow 2 \leq t \leq 4$