

3. (10 pts) (a) State the formal definition of "the function  $f$  is continuous at the point  $x = a$ ":

$$f \text{ is cont. at } x=a \text{ if } \lim_{x \rightarrow a} f(x) = f(a)$$

- (b) Using the definition, state why the function defined by  $f(x) = \begin{cases} \frac{x^2+5x-6}{1-x} & \text{if } x \neq 1 \\ -7 & \text{if } x = 1 \end{cases}$  is continuous at  $x = 1$ .

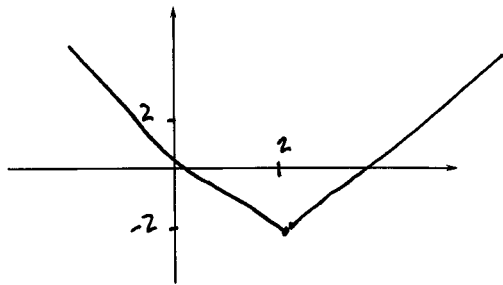
$$\text{observe: } \lim_{x \rightarrow 1} f(x) = \lim_{x \rightarrow 1} \left[ \frac{x^2+5x-6}{1-x} \right] = \lim_{x \rightarrow 1} \left[ \frac{(x-1)(x+6)}{1-x} \right]$$

$$= \lim_{x \rightarrow 1} [-x-6] = -7 = f(1)$$

so  $f$  is cont. at  $x=1$

4. (10 pts)

(a) Sketch the graph of  $f(x) = |x-2| - 2$ . sketch below.



(b) Determine if  $f(x)$  differentiable at every point and explain your reasoning.

no - the left hand limits and right hand limits of  $\frac{f(2+h) - f(2)}{h}$  don't agree